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' =============== Sub-procedures for ARDL unit root test =================
' ============== ARDL unit root test for no intercept model ================

if %selfspec = "N" then
    ' Determine the optimal lag length of ARDL model.
    if !maxlag = 0 then
        smpl %firstperiod %lastperiod
        equation eq_y.ls dy y(-1) x1(-1) c @trend
        table_aic_y(2,2) = eq_y.@aic
    else
        ' If maximum lag length more than 0, then determine the optimal model using algorithm below.
    if !maxlag > 0 then
        smpl %firstperiod %lastperiod
        equation eq_y.ls dy y(-1) x1(-1) c @trend       ' Calculate aic for ARDL(0,0) model.
        table_aic_y(2,2) = eq_y.@aic
        opt_aic_y = eq_y.@aic
        !opt_p = 0                                     ' Optimal lag length for dy.
        !opt_q = 0                                     ' Optimal lag length for dx.

        for !q=1 to !maxlag      ' Calculate the aic for 0 lag length for dy.
        smpl %firstperiod %lastperiod
        equation eq_y.ls dy y(-1) x1(-1) dx1(-1 to -!q) c @trend
        table_aic_y(2,2+!q) = eq_y.@aic
            if table_aic_y(2,2+!q) < opt_aic_y then
            opt_aic_y = eq_y.@aic
            !opt_p = 0
            !opt_q = !q
            endif
        next

        for !p=1 to !maxlag      ' Calculate the aic for 0 lag length for dx.
        smpl %firstperiod %lastperiod
        equation eq_y.ls dy y(-1) x1(-1) dy(-1 to -!p) c @trend
        table_aic_y(2+!p,2) = eq_y.@aic
            if table_aic_y(2+!p, 2) < opt_aic_y then
            opt_aic_y = eq_y.@aic
            !opt_p = !p
            !opt_q = 0
            endif
        next

        for !p=1 to !maxlag ' Calculate the aic for ARDL(m,n) model.
        for !q=1 to !maxlag
        smpl %firstperiod %lastperiod
        equation eq_y.ls dy y(-1) x1(-1) dy(-1 to -!p) dx1(-1 to -!q) c @trend
        table_aic_y(2+!p, 2+!q) = eq_y.@aic
            if table_aic_y(2+!p,2+!q) < opt_aic_y then
            opt_aic_y = eq_y.@aic
            !opt_p = !p
            !opt_q = !q
            endif
        next
        next
    endif
    endif

else
if %selfspec = "Y" then
    !opt_p = !fix_p
    !opt_q = !fix_q
endif
endif
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```
' Determine the longest lag length of the opimal model.
if !opt_p >= !opt_q then
!opt_lag = !opt_p
else
if !opt_p <= !opt_q then
!opt_lag = !opt_q
endif
endif

table(1,1) check_opt_ardl                    ' Check the optimal lag length for the ARDL.
setcell(check_opt_ardl, 1, 1, "ARDL(" + @str(!opt_p) + ", " + @str(!opt_q) + ")")

if !opt_p = 0 and !opt_q = 0 then
%cond_y = "00"
else
if !opt_p = 0 and !opt_q <> 0 then
%cond_y = "01"
else
if !opt_p <> 0 and !opt_q = 0 then
%cond_y = "10"
else
if !opt_p <> 0 and !opt_q <> 0 then
%cond_y = "11"
endif
endif
endif
endif

if %cond_y = "00" then
    smpl %firstperiod %lastperiod
    equation eq_opt_y.ls dy y(-1) x1(-1) c @trend
    scalar tstat_y = eq_opt_y.@tstat(1)                ' Obtain the testing t statistic.
    freeze(mode=overwrite, fstat_x_table) eq_opt_y.wald c(2)=0
    scalar fstat_y = @val(fstat_x_table(7,2))          ' Obtain the testing F statistic.

    ' ============== Bootstrap start here ==========================
    smpl %firstperiod %lastperiod
    ' Estimate equation with restriction of null y(-1) for t test and x(-1) for F test.
    equation restricted_t_y.ls dy x1(-1) c @trend      ' Impose y(-1) = 0.
    equation restricted_f_y.ls dy y(-1) c @trend       ' Impose x(-1) = 0.

    restricted_t_y.makeresids resids_t_y
    restricted_f_y.makeresids resids_f_y

    ' Recenter residuals
    scalar sum_resids_t_y = @csum(resids_t_y)
    scalar sum_resids_f_y = @csum(resids_f_y)

    scalar nobs_t = resids_t_y.@obs
    scalar nobs_f = resids_f_y.@obs

    for !ic=@dtoo(%firstperiod) to @dtoo(%lastperiod)
    resids_t_y(!ic) = resids_t_y(!ic) - (sum_resids_t_y/nobs_t)
    resids_f_y(!ic) = resids_f_y(!ic) - (sum_resids_f_y/nobs_f)
    next

    for !id=1 to 3
    vector(3) coef_restrict_t_y(!id) = restricted_t_y.@coef(!id)
    next

    for !ie=1 to 3
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    vector(3) coef_restrict_f_y(!ie) = restricted_f_y.@coef(!ie)
    next

    ' ========== Bootstrap replication start here ==================
    for !ib=1 to !nrep_b                    ' Bootstrap replication set for 10,000.
    smpl @all
    series y_t_b = y
    series dy_t_b = dy

    series y_f_b = y
    series dy_f_b = dy

    group gu resids_t_y resids_f_y
    gu.resample(dropna, outsmpl=%firstperiod %lastperiod, name=gu_b)

model a
    !start = @dtoo(%firstperiod) + 1
    %start = @otod(!start)
    smpl %start %lastperiod

    a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + coef_restrict_t_y(2) + coef_restrict_t_y(3)*@trend + resids_t_y_b
    a.append y_t_b = y_t_b(-1) + dy_t_b

    a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + coef_restrict_f_y(2) + coef_restrict_f_y(3)*@trend +
resids_f_y_b
    a.append y_f_b = y_f_b(-1) + dy_f_b

    a.scenario "actuals"
    a.solve

    smpl %firstperiod %lastperiod
    equation bootstrap_t_y.ls dy_t_b y_t_b(-1) x1(-1) c @trend
    scalar tstat_b = bootstrap_t_y.@tstat(1)

    tstat_b_dist(!ib) = tstat_b

    smpl %firstperiod %lastperiod
    equation bootstrap_f_y.ls dy_f_b y_f_b(-1) x1(-1) c @trend
    freeze(mode=overwrite,  fstat_x_b_table) bootstrap_f_y.wald c(2)=0
    scalar fstat_b = @val(fstat_x_b_table(7,2))

    fstat_b_dist(!ib) = fstat_b
    next
else
if %cond_y = "01" then
    smpl %firstperiod %lastperiod
    equation eq_opt_y.ls dy y(-1) x1(-1) dx1(-1 to -!opt_q) c @trend
    scalar tstat_y = eq_opt_y.@tstat(1)                 ' Obtain the testing t statistic.
    freeze(mode=overwrite, fstat_x_table) eq_opt_y.wald c(2)=0
    scalar fstat_y = @val(fstat_x_table(7,2))           ' Obtain the testing F statistic.

    ' ============== Bootstrap start here =========================
    smpl %firstperiod %lastperiod
    ' Estimate equation with restriction of null y(-1) for t test and x(-1) for F test.
    equation restricted_t_y.ls dy x1(-1) dx1(-1 to -!opt_q) c @trend        ' Impose y(-1) = 0.
    equation restricted_f_y.ls dy y(-1) dx1(-1 to -!opt_q) c @trend     ' Impose x(-1) = 0.

    restricted_t_y.makeresids resids_t_y
    restricted_f_y.makeresids resids_f_y

    ' Recenter residuals
    scalar sum_resids_t_y = @csum(resids_t_y)
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    scalar sum_resids_f_y = @csum(resids_f_y)

    scalar nobs_t = resids_t_y.@obs
    scalar nobs_f = resids_f_y.@obs

    for !c=@dtoo(%firstperiod) to @dtoo(%lastperiod)
    resids_t_y(!c) = resids_t_y(!c) - (sum_resids_t_y/nobs_t)
    resids_f_y(!c) = resids_f_y(!c) - (sum_resids_f_y/nobs_f)
    next

    !in = 3+!opt_q        ' Number of parameters in the restricted regression.
    for !id=1 to !in
    vector(!id) coef_restrict_t_y(!id) = restricted_t_y.@coef(!id)
    next

    for !ie=1 to !in
    vector(!ie) coef_restrict_f_y(!ie) = restricted_f_y.@coef(!ie)
    next

    ' ========== Bootstrap replication start here ==================
    for !ib=1 to !nrep_b                    ' Bootstrap replication set for 10,000.
    smpl @all
    series y_t_b = y
    series dy_t_b = dy
    series dify_t_b = 0

    series y_f_b = y
    series dy_f_b = dy
    series dify_f_b = 0

    group gu resids_t_y resids_f_y
    gu.resample(dropna, outsmpl=%firstperiod %lastperiod, name=gu_b)

    model a
    !start = @dtoo(%firstperiod) + !opt_lag + 1
    %start = @otod(!start)
    smpl %start %lastperiod
    if !opt_q = 1 then
        a.append dify_t_b = coef_restrict_t_y(2)*dx1(-1)

        a.append dify_f_b = coef_restrict_f_y(2)*dx1(-1)
    else
    if !opt_q = 2 then
        a.append dify_t_b = coef_restrict_t_y(2)*dx1(-1) + coef_restrict_t_y(3)*dx1(-2)

        a.append dify_f_b = coef_restrict_f_y(2)*dx1(-1) + coef_restrict_f_y(3)*dx1(-2)
    else
    if !opt_q = 3 then
        a.append dify_t_b = coef_restrict_t_y(2)*dx1(-1) + coef_restrict_t_y(3)*dx1(-2) + coef_restrict_t_y(4)*dx1(-3)

        a.append dify_f_b = coef_restrict_f_y(2)*dx1(-1) + coef_restrict_f_y(3)*dx1(-2) + coef_restrict_f_y(4)*dx1(-3)
    else
    if !opt_q = 4 then
        a.append dify_t_b = coef_restrict_t_y(2)*dx1(-1) + coef_restrict_t_y(3)*dx1(-2) + coef_restrict_t_y(4)*dx1(-3) +
coef_restrict_t_y(5)*dx1(-4)

        a.append dify_f_b = coef_restrict_f_y(2)*dx1(-1) + coef_restrict_f_y(3)*dx1(-2) + coef_restrict_f_y(4)*dx1(-3) +
coef_restrict_f_y(5)*dx1(-4)
    else
    if !opt_q = 5 then
        a.append dify_t_b = coef_restrict_t_y(2)*dx1(-1) + coef_restrict_t_y(3)*dx1(-2) + coef_restrict_t_y(4)*dx1(-3) +
coef_restrict_t_y(5)*dx1(-4) + coef_restrict_t_y(6)*dx1(-5)
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        a.append dify_f_b = coef_restrict_f_y(2)*dx1(-1) + coef_restrict_f_y(3)*dx1(-2) + coef_restrict_f_y(4)*dx1(-3) +
coef_restrict_f_y(5)*dx1(-4) + coef_restrict_f_y(6)*dx1(-5)
    else
    if !opt_q = 6 then
        a.append dify_t_b = coef_restrict_t_y(2)*dx1(-1) + coef_restrict_t_y(3)*dx1(-2) + coef_restrict_t_y(4)*dx1(-3) +
coef_restrict_t_y(5)*dx1(-4) + coef_restrict_t_y(6)*dx1(-5) + coef_restrict_t_y(7)*dx1(-6)

        a.append dify_f_b = coef_restrict_f_y(2)*dx1(-1) + coef_restrict_f_y(3)*dx1(-2) + coef_restrict_f_y(4)*dx1(-3) +
coef_restrict_f_y(5)*dx1(-4) + coef_restrict_f_y(6)*dx1(-5) + coef_restrict_f_y(7)*dx1(-6)
    else
    if !opt_q = 7 then
        a.append dify_t_b = coef_restrict_t_y(2)*dx1(-1) + coef_restrict_t_y(3)*dx1(-2) + coef_restrict_t_y(4)*dx1(-3) +
coef_restrict_t_y(5)*dx1(-4) + coef_restrict_t_y(6)*dx1(-5) + coef_restrict_t_y(7)*dx1(-6) + coef_restrict_t_y(8)*dx1(-7)

        a.append dify_f_b = coef_restrict_f_y(2)*dx1(-1) + coef_restrict_f_y(3)*dx1(-2) + coef_restrict_f_y(4)*dx1(-3) +
coef_restrict_f_y(5)*dx1(-4) + coef_restrict_f_y(6)*dx1(-5) + coef_restrict_f_y(7)*dx1(-6) + coef_restrict_f_y(8)*dx1(-7)
    else
    if !opt_q = 8 then
        a.append dify_t_b = coef_restrict_t_y(2)*dx1(-1) + coef_restrict_t_y(3)*dx1(-2) + coef_restrict_t_y(4)*dx1(-3) +
coef_restrict_t_y(5)*dx1(-4) + coef_restrict_t_y(6)*dx1(-5) + coef_restrict_t_y(7)*dx1(-6) + coef_restrict_t_y(8)*dx1(-7)
+ coef_restrict_t_y(9)*dx1(-8)

        a.append dify_f_b = coef_restrict_f_y(2)*dx1(-1) + coef_restrict_f_y(3)*dx1(-2) + coef_restrict_f_y(4)*dx1(-3) +
coef_restrict_f_y(5)*dx1(-4) + coef_restrict_f_y(6)*dx1(-5) + coef_restrict_f_y(7)*dx1(-6) + coef_restrict_f_y(8)*dx1(-7)
+ coef_restrict_f_y(9)*dx1(-8)
    else
    if !opt_q = 9 then
        a.append dify_t_b = coef_restrict_t_y(2)*dx1(-1) + coef_restrict_t_y(3)*dx1(-2) + coef_restrict_t_y(4)*dx1(-3) +
coef_restrict_t_y(5)*dx1(-4) + coef_restrict_t_y(6)*dx1(-5) + coef_restrict_t_y(7)*dx1(-6) + coef_restrict_t_y(8)*dx1(-7)
+ coef_restrict_t_y(9)*dx1(-8) + coef_restrict_t_y(10)*dx1(-9)

        a.append dify_f_b = coef_restrict_f_y(2)*dx1(-1) + coef_restrict_f_y(3)*dx1(-2) + coef_restrict_f_y(4)*dx1(-3) +
coef_restrict_f_y(5)*dx1(-4) + coef_restrict_f_y(6)*dx1(-5) + coef_restrict_f_y(7)*dx1(-6) + coef_restrict_f_y(8)*dx1(-7)
+ coef_restrict_f_y(9)*dx1(-8) + coef_restrict_f_y(10)*dx1(-9)
    else
    if !opt_q = 10 then
        a.append dify_f_b = coef_restrict_f_y(2)*dx1(-1) + coef_restrict_f_y(3)*dx1(-2) + coef_restrict_f_y(4)*dx1(-3) +
coef_restrict_f_y(5)*dx1(-4) + coef_restrict_f_y(6)*dx1(-5) + coef_restrict_f_y(7)*dx1(-6) + coef_restrict_f_y(8)*dx1(-7)
+ coef_restrict_f_y(9)*dx1(-8) + coef_restrict_f_y(10)*dx1(-9) + coef_restrict_f_y(11)*dx1(-10)
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif

if !opt_q = 1 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(3) + coef_restrict_t_y(4)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(3) + coef_restrict_f_y(4)*@trend +
resids_f_y_b
else
if !opt_q = 2 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(4) + coef_restrict_t_y(5)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(4) + coef_restrict_f_y(5)*@trend +
resids_f_y_b
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else
if !opt_q = 3 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(5) + coef_restrict_t_y(6)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(5) + coef_restrict_f_y(6)*@trend +
resids_f_y_b
else
if !opt_q = 4 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(6) + coef_restrict_t_y(7)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(6) + coef_restrict_f_y(7)*@trend +
resids_f_y_b
else
if !opt_q = 5 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(7) + coef_restrict_t_y(8)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(7) + coef_restrict_f_y(8)*@trend +
resids_f_y_b
else
if !opt_q = 6 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(8) + coef_restrict_t_y(9)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(8) + coef_restrict_f_y(9)*@trend +
resids_f_y_b
else
if !opt_q = 7 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(9) + coef_restrict_t_y(10)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(9) + coef_restrict_f_y(10)*@trend +
resids_f_y_b
else
if !opt_q = 8 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(10) + coef_restrict_t_y(11)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(10) + coef_restrict_f_y(11)*@trend +
resids_f_y_b
else
if !opt_q = 9 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(11) + coef_restrict_t_y(12)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(11) + coef_restrict_f_y(12)*@trend +
resids_f_y_b
else
if !opt_q = 10 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(12) + coef_restrict_t_y(13)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(12) + coef_restrict_f_y(13)*@trend +
resids_f_y_b
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif

a.append y_t_b = y_t_b(-1) + dy_t_b
a.append y_f_b = y_f_b(-1) + dy_f_b
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```
a.scenario "actuals"
a.solve

    smpl %firstperiod %lastperiod
    equation bootstrap_t_y.ls dy_t_b y_t_b(-1) x1(-1) dx1(-1 to -!opt_q) c @trend
    scalar tstat_b = bootstrap_t_y.@tstat(1)

    tstat_b_dist(!ib) = tstat_b

    smpl %firstperiod %lastperiod
    equation bootstrap_f_y.ls dy_f_b y_f_b(-1) x1(-1) dx1(-1 to -!opt_q) c @trend
    freeze(mode=overwrite,  fstat_x_b_table) bootstrap_f_y.wald c(2)=0
    scalar fstat_b = @val(fstat_x_b_table(7,2))

    fstat_b_dist(!ib) = fstat_b
    next
else
if %cond_y = "10" then
    smpl %firstperiod %lastperiod
    equation eq_opt_y.ls dy y(-1) x1(-1) dy(-1 to -!opt_p) c @trend
    scalar tstat_y = eq_opt_y.@tstat(1)                    ' Obtain the testing t statistic.
    freeze(mode=overwrite, fstat_x_table) eq_opt_y.wald c(2)=0
    scalar fstat_y = @val(fstat_x_table(7,2))              ' Obtain the testing F statistic.

    ' ============== Bootstrap start here ==========================
    smpl %firstperiod %lastperiod
    ' Estimate equation with restriction of null y(-1) for t test and x(-1) for F test.
    equation restricted_t_y.ls dy x1(-1) dy(-1 to -!opt_p) c @trend          ' Impose y(-1) = 0.
    equation restricted_f_y.ls dy y(-1) dy(-1 to -!opt_p) c @trend           ' Impose x(-1) = 0.

    restricted_t_y.makeresids resids_t_y
    restricted_f_y.makeresids resids_f_y

    ' Recenter residuals
    scalar sum_resids_t_y = @csum(resids_t_y)
    scalar sum_resids_f_y = @csum(resids_f_y)

    scalar nobs_t = resids_t_y.@obs
    scalar nobs_f = resids_f_y.@obs

    for !c=@dtoo(%firstperiod) to @dtoo(%lastperiod)
    resids_t_y(!c) = resids_t_y(!c) - (sum_resids_t_y/nobs_t)
    resids_f_y(!c) = resids_f_y(!c) - (sum_resids_f_y/nobs_f)
    next

    !in = 3+!opt_p          ' Number of parameters in the restricted regression.
    for !id=1 to !in
    vector(!id) coef_restrict_t_y(!id) = restricted_t_y.@coef(!id)
    next

    for !ie=1 to !in
    vector(!ie) coef_restrict_f_y(!ie) = restricted_f_y.@coef(!ie)
    next

    ' ============ Bootstrap replication start here ==================
'   pagestruct(end = 5000+@dtoo(%lastperiod))
    for !ib=1 to !nrep_b                ' Bootstrap replication set for 10,000.
    smpl @all
    series y_t_b = y
    series dy_t_b = dy
    series dify_t_b = 0
```

```
    series y_f_b = y
    series dy_f_b = dy
    series dify_f_b = 0

    group gu resids_t_y resids_f_y
    gu.resample(dropna, outsmpl=%firstperiod %lastperiod, name=gu_b)

model a
    !start = @dtoo(%firstperiod) + !opt_lag + 1
    %start = @otod(!start)
    smpl %start %lastperiod
    if !opt_p = 1 then
        a.append dify_t_b = coef_restrict_t_y(2)*dy_t_b(-1)

        a.append dify_f_b = coef_restrict_f_y(2)*dy_f_b(-1)
    else
    if !opt_p = 2 then
        a.append dify_t_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2)

        a.append dify_f_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2)
    else
    if !opt_p = 3 then
        a.append dify_t_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2) +
coef_restrict_t_y(4)*dy_t_b(-3)

        a.append dify_f_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2) +
coef_restrict_f_y(4)*dy_f_b(-3)
    else
    if !opt_p = 4 then
        a.append dify_t_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2) +
coef_restrict_t_y(4)*dy_t_b(-3) + coef_restrict_t_y(5)*dy_t_b(-4)

        a.append dify_f_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2) +
coef_restrict_f_y(4)*dy_f_b(-3) + coef_restrict_f_y(5)*dy_f_b(-4)
    else
    if !opt_p = 5 then
        a.append dify_t_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2) +
coef_restrict_t_y(4)*dy_t_b(-3) + coef_restrict_t_y(5)*dy_t_b(-4) + coef_restrict_t_y(6)*dy_t_b(-5)

        a.append dify_f_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2) +
coef_restrict_f_y(4)*dy_f_b(-3) + coef_restrict_f_y(5)*dy_f_b(-4) + coef_restrict_f_y(6)*dy_f_b(-5)
    else
    if !opt_p = 6 then
        a.append dify_t_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2) +
coef_restrict_t_y(4)*dy_t_b(-3) + coef_restrict_t_y(5)*dy_t_b(-4) + coef_restrict_t_y(6)*dy_t_b(-5) +
coef_restrict_t_y(7)*dy_t_b(-6)

        a.append dify_f_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2) +
coef_restrict_f_y(4)*dy_f_b(-3) + coef_restrict_f_y(5)*dy_f_b(-4) + coef_restrict_f_y(6)*dy_f_b(-5) +
coef_restrict_f_y(7)*dy_f_b(-6)
    else
    if !opt_p = 7 then
        a.append dify_t_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2) +
coef_restrict_t_y(4)*dy_t_b(-3) + coef_restrict_t_y(5)*dy_t_b(-4) + coef_restrict_t_y(6)*dy_t_b(-5) +
coef_restrict_t_y(7)*dy_t_b(-6) + coef_restrict_t_y(8)*dy_t_b(-7)

        a.append dify_f_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2) +
coef_restrict_f_y(4)*dy_f_b(-3) + coef_restrict_f_y(5)*dy_f_b(-4) + coef_restrict_f_y(6)*dy_f_b(-5) +
coef_restrict_f_y(7)*dy_f_b(-6) + coef_restrict_f_y(8)*dy_f_b(-7)
    else
    if !opt_p = 8 then
```

```
        a.append dify_t_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2) +
coef_restrict_t_y(4)*dy_t_b(-3) + coef_restrict_t_y(5)*dy_t_b(-4) + coef_restrict_t_y(6)*dy_t_b(-5) +
coef_restrict_t_y(7)*dy_t_b(-6) + coef_restrict_t_y(8)*dy_t_b(-7) + coef_restrict_t_y(9)*dy_t_b(-8)

        a.append dify_f_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2) +
coef_restrict_f_y(4)*dy_f_b(-3) + coef_restrict_f_y(5)*dy_f_b(-4) + coef_restrict_f_y(6)*dy_f_b(-5) +
coef_restrict_f_y(7)*dy_f_b(-6) + coef_restrict_f_y(8)*dy_f_b(-7) + coef_restrict_f_y(9)*dy_f_b(-8)
    else
    if !opt_p = 9 then
        a.append dify_t_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2) +
coef_restrict_t_y(4)*dy_t_b(-3) + coef_restrict_t_y(5)*dy_t_b(-4) + coef_restrict_t_y(6)*dy_t_b(-5) +
coef_restrict_t_y(7)*dy_t_b(-6) + coef_restrict_t_y(8)*dy_t_b(-7) + coef_restrict_t_y(9)*dy_t_b(-8) +
coef_restrict_t_y(10)*dy_t_b(-9)

        a.append dify_f_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2) +
coef_restrict_f_y(4)*dy_f_b(-3) + coef_restrict_f_y(5)*dy_f_b(-4) + coef_restrict_f_y(6)*dy_f_b(-5) +
coef_restrict_f_y(7)*dy_f_b(-6) + coef_restrict_f_y(8)*dy_f_b(-7) + coef_restrict_f_y(9)*dy_f_b(-8) +
coef_restrict_f_y(10)*dy_f_b(-9)
    else
    if !opt_p = 10 then
        a.append dify_t_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2) +
coef_restrict_t_y(4)*dy_t_b(-3) + coef_restrict_t_y(5)*dy_t_b(-4) + coef_restrict_t_y(6)*dy_t_b(-5) +
coef_restrict_t_y(7)*dy_t_b(-6) + coef_restrict_t_y(8)*dy_t_b(-7) + coef_restrict_t_y(9)*dy_t_b(-8) +
coef_restrict_t_y(10)*dy_t_b(-9) + coef_restrict_t_y(11)*dy_t_b(-10)

        a.append dify_f_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2) +
coef_restrict_f_y(4)*dy_f_b(-3) + coef_restrict_f_y(5)*dy_f_b(-4) + coef_restrict_f_y(6)*dy_f_b(-5) +
coef_restrict_f_y(7)*dy_f_b(-6) + coef_restrict_f_y(8)*dy_f_b(-7) + coef_restrict_f_y(9)*dy_f_b(-8) +
coef_restrict_f_y(10)*dy_f_b(-9) + coef_restrict_f_y(11)*dy_f_b(-10)
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif

if !opt_p = 1 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(3) + coef_restrict_t_y(4)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(3) + coef_restrict_f_y(4)*@trend +
resids_f_y_b
else
if !opt_p = 2 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(4) + coef_restrict_t_y(5)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(4) + coef_restrict_f_y(5)*@trend +
resids_f_y_b
else
if !opt_p = 3 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(5) + coef_restrict_t_y(6)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(5) + coef_restrict_f_y(6)*@trend +
resids_f_y_b
else
if !opt_p = 4 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(6) + coef_restrict_t_y(7)*@trend +
resids_t_y_b
```

```
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(6) + coef_restrict_f_y(7)*@trend +
resids_f_y_b
else
if !opt_p = 5 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(7) + coef_restrict_t_y(8)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(7) + coef_restrict_f_y(8)*@trend +
resids_f_y_b
else
if !opt_p = 6 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(8) + coef_restrict_t_y(9)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(8) + coef_restrict_f_y(9)*@trend +
resids_f_y_b
else
if !opt_p = 7 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(9) + coef_restrict_t_y(10)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(9) + coef_restrict_f_y(10)*@trend +
resids_f_y_b
else
if !opt_p = 8 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(10) + coef_restrict_t_y(11)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(10) + coef_restrict_f_y(11)*@trend +
resids_f_y_b
else
if !opt_p = 9 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(11) + coef_restrict_t_y(12)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(11) + coef_restrict_f_y(12)*@trend +
resids_f_y_b
else
if !opt_p = 10 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_t_b + coef_restrict_t_y(12) + coef_restrict_t_y(13)*@trend +
resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_f_b + coef_restrict_f_y(12) + coef_restrict_f_y(13)*@trend +
resids_f_y_b
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif

a.append y_t_b = y_t_b(-1) + dy_t_b
a.append y_f_b = y_f_b(-1) + dy_f_b

a.scenario "actuals"
a.solve

    smpl %firstperiod %lastperiod
    equation bootstrap_t_y.ls dy_t_b y_t_b(-1) x1(-1) dy_t_b(-1 to -!opt_p) c @trend
    scalar tstat_b = bootstrap_t_y.@tstat(1)

    tstat_b_dist(!ib) = tstat_b

    smpl %firstperiod %lastperiod
```

```
    equation bootstrap_f_y.ls dy_f_b y_f_b(-1) x1(-1) dy_f_b(-1 to -!opt_p) c @trend
    freeze(mode=overwrite,  fstat_x_b_table) bootstrap_f_y.wald c(2)=0
    scalar fstat_b = @val(fstat_x_b_table(7,2))

    fstat_b_dist(!ib) = fstat_b
    next
else
if %cond_y = "11" then
    smpl %firstperiod %lastperiod
    equation eq_opt_y.ls dy y(-1) x1(-1) dy(-1 to -!opt_p) dx1(-1 to -!opt_q) c @trend
    scalar tstat_y = eq_opt_y.@tstat(1)                    ' Obtain the testing t statistic.
    freeze(mode=overwrite, fstat_x_table) eq_opt_y.wald c(2)=0
    scalar fstat_y = @val(fstat_x_table(7,2))              ' Obtain the testing F statistic.

    ' ============== Bootstrap start here ========================
    smpl %firstperiod %lastperiod
    ' Estimate equation with restriction of null y(-1) for t test and x(-1) for F test.
    equation restricted_t_y.ls dy x1(-1) dy(-1 to -!opt_p) dx1(-1 to -!opt_q) c @trend          ' Impose y(-1) = 0.
    equation restricted_f_y.ls dy y(-1) dy(-1 to -!opt_p)   dx1(-1 to -!opt_q) c @trend         ' Impose x(-1) = 0.

    restricted_t_y.makeresids resids_t_y
    restricted_f_y.makeresids resids_f_y

    ' Recenter residuals
    scalar sum_resids_t_y = @csum(resids_t_y)
    scalar sum_resids_f_y = @csum(resids_f_y)

    scalar nobs_t = resids_t_y.@obs
    scalar nobs_f = resids_f_y.@obs

    for !c=@dtoo(%firstperiod) to @dtoo(%lastperiod)
    resids_t_y(!c) = resids_t_y(!c) - (sum_resids_t_y/nobs_t)
    resids_f_y(!c) = resids_f_y(!c) - (sum_resids_f_y/nobs_f)
    next

    !in = 3+!opt_p+!opt_q          ' Number of parameters in the restricted regression.
    for !id=1 to !in
    vector(!id) coef_restrict_t_y(!id) = restricted_t_y.@coef(!id)
    next

    for !ie=1 to !in
    vector(!ie) coef_restrict_f_y(!ie) = restricted_f_y.@coef(!ie)
    next

    ' ========== Bootstrap replication start here ================
    for !ib=1 to !nrep_b                ' Bootstrap replication set for 10,000.
    smpl @all
    series y_t_b = y
    series dy_t_b = dy
    series dify_ty_b = 0
    series dif_tx_b = 0

    series y_f_b = y
    series dy_f_b = dy
    series dify_fy_b = 0
    series dify_fx_b = 0

    group gu resids_t_y resids_f_y
    gu.resample(dropna, outsmpl=%firstperiod %lastperiod, name=gu_b)

    !totallag = !opt_p + !opt_q          ' Total lags for the differenced terms.
```

```
model a
    !start = @dtoo(%firstperiod) + !opt_lag + 1
    %start = @otod(!start)
    smpl %start %lastperiod
    if !opt_p = 1 then
        a.append dify_ty_b = coef_restrict_t_y(2)*dy_t_b(-1)
    else
    if !opt_p = 2 then
        a.append dify_ty_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2)
    else
    if !opt_p = 3 then
        a.append dify_ty_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2) +
coef_restrict_t_y(4)*dy_t_b(-3)
    else
    if !opt_p = 4 then
        a.append dify_ty_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2) +
coef_restrict_t_y(4)*dy_t_b(-3) + coef_restrict_t_y(5)*dy_t_b(-4)
    else
    if !opt_p = 5 then
        a.append dify_ty_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2) +
coef_restrict_t_y(4)*dy_t_b(-3) + coef_restrict_t_y(5)*dy_t_b(-4) + coef_restrict_t_y(6)*dy_t_b(-5)
    else
    if !opt_p = 6 then
        a.append dify_ty_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2) +
coef_restrict_t_y(4)*dy_t_b(-3) + coef_restrict_t_y(5)*dy_t_b(-4) + coef_restrict_t_y(6)*dy_t_b(-5) +
coef_restrict_t_y(7)*dy_t_b(-6)
    else
    if !opt_p = 7 then
        a.append dify_ty_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2) +
coef_restrict_t_y(4)*dy_t_b(-3) + coef_restrict_t_y(5)*dy_t_b(-4) + coef_restrict_t_y(6)*dy_t_b(-5) +
coef_restrict_t_y(7)*dy_t_b(-6) + coef_restrict_t_y(8)*dy_t_b(-7)
    else
    if !opt_p = 8 then
        a.append dify_ty_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2) +
coef_restrict_t_y(4)*dy_t_b(-3) + coef_restrict_t_y(5)*dy_t_b(-4) + coef_restrict_t_y(6)*dy_t_b(-5) +
coef_restrict_t_y(7)*dy_t_b(-6) + coef_restrict_t_y(8)*dy_t_b(-7) + coef_restrict_t_y(9)*dy_t_b(-8)
    else
    if !opt_p = 9 then
        a.append dify_ty_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2) +
coef_restrict_t_y(4)*dy_t_b(-3) + coef_restrict_t_y(5)*dy_t_b(-4) + coef_restrict_t_y(6)*dy_t_b(-5) +
coef_restrict_t_y(7)*dy_t_b(-6) + coef_restrict_t_y(8)*dy_t_b(-7) + coef_restrict_t_y(9)*dy_t_b(-8) +
coef_restrict_t_y(10)*dy_t_b(-9)
    else
    if !opt_p = 10 then
        a.append dify_ty_b = coef_restrict_t_y(2)*dy_t_b(-1) + coef_restrict_t_y(3)*dy_t_b(-2) +
coef_restrict_t_y(4)*dy_t_b(-3) + coef_restrict_t_y(5)*dy_t_b(-4) + coef_restrict_t_y(6)*dy_t_b(-5) +
coef_restrict_t_y(7)*dy_t_b(-6) + coef_restrict_t_y(8)*dy_t_b(-7) + coef_restrict_t_y(9)*dy_t_b(-8) +
coef_restrict_t_y(10)*dy_t_b(-9) + coef_restrict_t_y(11)*dy_t_b(-10)
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif

    if !opt_q = 1 then
        a.append dify_tx_b = coef_restrict_t_y(!opt_p+2)*dx1(-1)
    else
```

```
    if !opt_q = 2 then
        a.append dify_tx_b = coef_restrict_t_y(!opt_p+2)*dx1(-1) + coef_restrict_t_y(!opt_p+3)*dx1(-2)
    else
    if !opt_q = 3 then
        a.append dify_tx_b = coef_restrict_t_y(!opt_p+2)*dx1(-1) + coef_restrict_t_y(!opt_p+3)*dx1(-2) +
coef_restrict_t_y(!opt_p+4)*dx1(-3)
    else
    if !opt_q = 4 then
        a.append dify_tx_b = coef_restrict_t_y(!opt_p+2)*dx1(-1) + coef_restrict_t_y(!opt_p+3)*dx1(-2) +
coef_restrict_t_y(!opt_p+4)*dx1(-3) + coef_restrict_t_y(!opt_p+5)*dx1(-4)
    else
    if !opt_q = 5 then
        a.append dify_tx_b = coef_restrict_t_y(!opt_p+2)*dx1(-1) + coef_restrict_t_y(!opt_p+3)*dx1(-2) +
coef_restrict_t_y(!opt_p+4)*dx1(-3) + coef_restrict_t_y(!opt_p+5)*dx1(-4) + coef_restrict_t_y(!opt_p+6)*dx1(-5)
    else
    if !opt_q = 6 then
        a.append dify_tx_b = coef_restrict_t_y(!opt_p+2)*dx1(-1) + coef_restrict_t_y(!opt_p+3)*dx1(-2) +
coef_restrict_t_y(!opt_p+4)*dx1(-3) + coef_restrict_t_y(!opt_p+5)*dx1(-4) + coef_restrict_t_y(!opt_p+6)*dx1(-5) +
coef_restrict_t_y(!opt_p+7)*dx1(-6)
    else
    if !opt_q = 7 then
        a.append dify_tx_b = coef_restrict_t_y(!opt_p+2)*dx1(-1) + coef_restrict_t_y(!opt_p+3)*dx1(-2) +
coef_restrict_t_y(!opt_p+4)*dx1(-3) + coef_restrict_t_y(!opt_p+5)*dx1(-4) + coef_restrict_t_y(!opt_p+6)*dx1(-5) +
coef_restrict_t_y(!opt_p+7)*dx1(-6) + coef_restrict_t_y(!opt_p+8)*dx1(-7)
    else
    if !opt_q = 8 then
        a.append dify_tx_b = coef_restrict_t_y(!opt_p+2)*dx1(-1) + coef_restrict_t_y(!opt_p+3)*dx1(-2) +
coef_restrict_t_y(!opt_p+4)*dx1(-3) + coef_restrict_t_y(!opt_p+5)*dx1(-4) + coef_restrict_t_y(!opt_p+6)*dx1(-5) +
coef_restrict_t_y(!opt_p+7)*dx1(-6) + coef_restrict_t_y(!opt_p+8)*dx1(-7) + coef_restrict_t_y(!opt_p+9)*dx1(-8)
    else
    if !opt_q = 9 then
        a.append dify_tx_b = coef_restrict_t_y(!opt_p+2)*dx1(-1) + coef_restrict_t_y(!opt_p+3)*dx1(-2) +
coef_restrict_t_y(!opt_p+4)*dx1(-3) + coef_restrict_t_y(!opt_p+5)*dx1(-4) + coef_restrict_t_y(!opt_p+6)*dx1(-5) +
coef_restrict_t_y(!opt_p+7)*dx1(-6) + coef_restrict_t_y(!opt_p+8)*dx1(-7) + coef_restrict_t_y(!opt_p+9)*dx1(-8) +
coef_restrict_t_y(!opt_p+10)*dx1(-9)
    else
    if !opt_q = 10 then
        a.append dify_tx_b = coef_restrict_t_y(!opt_p+2)*dx1(-1) + coef_restrict_t_y(!opt_p+3)*dx1(-2) +
coef_restrict_t_y(!opt_p+4)*dx1(-3) + coef_restrict_t_y(!opt_p+5)*dx1(-4) + coef_restrict_t_y(!opt_p+6)*dx1(-5) +
coef_restrict_t_y(!opt_p+7)*dx1(-6) + coef_restrict_t_y(!opt_p+8)*dx1(-7) + coef_restrict_t_y(!opt_p+9)*dx1(-8) +
coef_restrict_t_y(!opt_p+10)*dx1(-9) + coef_restrict_t_y(!opt_p+11)*dx1(-10)
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif

    if !opt_p = 1 then
        a.append dify_fy_b = coef_restrict_f_y(2)*dy_f_b(-1)
    else
    if !opt_p = 2 then
        a.append dify_fy_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2)
    else
    if !opt_p = 3 then
        a.append dify_fy_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2) +
coef_restrict_f_y(4)*dy_f_b(-3)
    else
```

```
    if !opt_p = 4 then
        a.append dify_fy_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2) +
coef_restrict_f_y(4)*dy_f_b(-3) + coef_restrict_f_y(5)*dy_f_b(-4)
    else
    if !opt_p = 5 then
        a.append dify_fy_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2) +
coef_restrict_f_y(4)*dy_f_b(-3) + coef_restrict_f_y(5)*dy_f_b(-4) + coef_restrict_f_y(6)*dy_f_b(-5)
    else
    if !opt_p = 6 then
        a.append dify_fy_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2) +
coef_restrict_f_y(4)*dy_f_b(-3) + coef_restrict_f_y(5)*dy_f_b(-4) + coef_restrict_f_y(6)*dy_f_b(-5) +
coef_restrict_f_y(7)*dy_f_b(-6)
    else
    if !opt_p = 7 then
        a.append dify_fy_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2) +
coef_restrict_f_y(4)*dy_f_b(-3) + coef_restrict_f_y(5)*dy_f_b(-4) + coef_restrict_f_y(6)*dy_f_b(-5) +
coef_restrict_f_y(7)*dy_f_b(-6) + coef_restrict_f_y(8)*dy_f_b(-7)
    else
    if !opt_p = 8 then
        a.append dify_fy_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2) +
coef_restrict_f_y(4)*dy_f_b(-3) + coef_restrict_f_y(5)*dy_f_b(-4) + coef_restrict_f_y(6)*dy_f_b(-5) +
coef_restrict_f_y(7)*dy_f_b(-6) + coef_restrict_f_y(8)*dy_f_b(-7) + coef_restrict_f_y(9)*dy_f_b(-8)
    else
    if !opt_p = 9 then
        a.append dify_fy_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2) +
coef_restrict_f_y(4)*dy_f_b(-3) + coef_restrict_f_y(5)*dy_f_b(-4) + coef_restrict_f_y(6)*dy_f_b(-5) +
coef_restrict_f_y(7)*dy_f_b(-6) + coef_restrict_f_y(8)*dy_f_b(-7) + coef_restrict_f_y(9)*dy_f_b(-8) +
coef_restrict_f_y(10)*dy_f_b(-9)
    else
    if !opt_p = 10 then
        a.append dify_fy_b = coef_restrict_f_y(2)*dy_f_b(-1) + coef_restrict_f_y(3)*dy_f_b(-2) +
coef_restrict_f_y(4)*dy_f_b(-3) + coef_restrict_f_y(5)*dy_f_b(-4) + coef_restrict_f_y(6)*dy_f_b(-5) +
coef_restrict_f_y(7)*dy_f_b(-6) + coef_restrict_f_y(8)*dy_f_b(-7) + coef_restrict_f_y(9)*dy_f_b(-8) +
coef_restrict_f_y(10)*dy_f_b(-9) + coef_restrict_f_y(11)*dy_f_b(-10)
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif

    if !opt_q = 1 then
        a.append dify_fx_b = coef_restrict_f_y(!opt_p+2)*dx1(-1)
    else
    if !opt_q = 2 then
        a.append dify_fx_b = coef_restrict_f_y(!opt_p+2)*dx1(-1) + coef_restrict_f_y(!opt_p+3)*dx1(-2)
    else
    if !opt_q = 3 then
        a.append dify_fx_b = coef_restrict_f_y(!opt_p+2)*dx1(-1) + coef_restrict_f_y(!opt_p+3)*dx1(-2) +
coef_restrict_f_y(!opt_p+4)*dx1(-3)
    else
    if !opt_q = 4 then
        a.append dify_fx_b = coef_restrict_f_y(!opt_p+2)*dx1(-1) + coef_restrict_f_y(!opt_p+3)*dx1(-2) +
coef_restrict_f_y(!opt_p+4)*dx1(-3) + coef_restrict_f_y(!opt_p+5)*dx1(-4)
    else
    if !opt_q = 5 then
        a.append dify_fx_b = coef_restrict_f_y(!opt_p+2)*dx1(-1) + coef_restrict_f_y(!opt_p+3)*dx1(-2) +
coef_restrict_f_y(!opt_p+4)*dx1(-3) + coef_restrict_f_y(!opt_p+5)*dx1(-4) + coef_restrict_f_y(!opt_p+6)*dx1(-5)
```

```
    else
    if !opt_q = 6 then
        a.append dify_fx_b = coef_restrict_f_y(!opt_p+2)*dx1(-1) + coef_restrict_f_y(!opt_p+3)*dx1(-2) +
coef_restrict_f_y(!opt_p+4)*dx1(-3) + coef_restrict_f_y(!opt_p+5)*dx1(-4) + coef_restrict_f_y(!opt_p+6)*dx1(-5) +
coef_restrict_f_y(!opt_p+7)*dx1(-6)
    else
    if !opt_q = 7 then
        a.append dify_fx_b = coef_restrict_f_y(!opt_p+2)*dx1(-1) + coef_restrict_f_y(!opt_p+3)*dx1(-2) +
coef_restrict_f_y(!opt_p+4)*dx1(-3) + coef_restrict_f_y(!opt_p+5)*dx1(-4) + coef_restrict_f_y(!opt_p+6)*dx1(-5) +
coef_restrict_f_y(!opt_p+7)*dx1(-6) + coef_restrict_f_y(!opt_p+8)*dx1(-7)
    else
    if !opt_q = 8 then
        a.append dify_fx_b = coef_restrict_f_y(!opt_p+2)*dx1(-1) + coef_restrict_f_y(!opt_p+3)*dx1(-2) +
coef_restrict_f_y(!opt_p+4)*dx1(-3) + coef_restrict_f_y(!opt_p+5)*dx1(-4) + coef_restrict_f_y(!opt_p+6)*dx1(-5) +
coef_restrict_f_y(!opt_p+7)*dx1(-6) + coef_restrict_f_y(!opt_p+8)*dx1(-7) + coef_restrict_f_y(!opt_p+9)*dx1(-8)
    else
    if !opt_q = 9 then
        a.append dify_fx_b = coef_restrict_f_y(!opt_p+2)*dx1(-1) + coef_restrict_f_y(!opt_p+3)*dx1(-2) +
coef_restrict_f_y(!opt_p+4)*dx1(-3) + coef_restrict_f_y(!opt_p+5)*dx1(-4) + coef_restrict_f_y(!opt_p+6)*dx1(-5) +
coef_restrict_f_y(!opt_p+7)*dx1(-6) + coef_restrict_f_y(!opt_p+8)*dx1(-7) + coef_restrict_f_y(!opt_p+9)*dx1(-8) +
coef_restrict_f_y(!opt_p+10)*dx1(-9)
    else
    if !opt_q = 10 then
        a.append dify_fx_b = coef_restrict_f_y(!opt_p+2)*dx1(-1) + coef_restrict_f_y(!opt_p+3)*dx1(-2) +
coef_restrict_f_y(!opt_p+4)*dx1(-3) + coef_restrict_f_y(!opt_p+5)*dx1(-4) + coef_restrict_f_y(!opt_p+6)*dx1(-5) +
coef_restrict_f_y(!opt_p+7)*dx1(-6) + coef_restrict_f_y(!opt_p+8)*dx1(-7) + coef_restrict_f_y(!opt_p+9)*dx1(-8) +
coef_restrict_f_y(!opt_p+10)*dx1(-9) + coef_restrict_f_y(!opt_p+11)*dx1(-10)
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif

if !totallag = 2 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(4) +
coef_restrict_t_y(5)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(4) +
coef_restrict_f_y(5)*@trend + resids_f_y_b
else
if !totallag = 3 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(5) +
coef_restrict_t_y(6)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(5) +
coef_restrict_f_y(6)*@trend + resids_f_y_b
else
if !totallag = 4 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(6) +
coef_restrict_t_y(7)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(6) +
coef_restrict_f_y(7)*@trend + resids_f_y_b
else
if !totallag = 5 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(7) +
coef_restrict_t_y(8)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(7) +
coef_restrict_f_y(8)*@trend + resids_f_y_b
else
```

```
if !totallag = 6 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(8) +
coef_restrict_t_y(9)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(8) +
coef_restrict_f_y(9)*@trend + resids_f_y_b
else
if !totallag = 7 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(9) +
coef_restrict_t_y(10)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(9) +
coef_restrict_f_y(10)*@trend + resids_f_y_b
else
if !totallag = 8 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(10) +
coef_restrict_t_y(11)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(10) +
coef_restrict_f_y(11)*@trend + resids_f_y_b
else
if !totallag = 9 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(11) +
coef_restrict_t_y(12)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(11) +
coef_restrict_f_y(12)*@trend + resids_f_y_b
else
if !totallag = 10 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(12) +
coef_restrict_t_y(13)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(12) +
coef_restrict_f_y(13)*@trend + resids_f_y_b
else
if !totallag = 11 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(13) +
coef_restrict_t_y(14)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(13) +
coef_restrict_f_y(14)*@trend + resids_f_y_b
else
if !totallag = 12 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(14) +
coef_restrict_t_y(15)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(14) +
coef_restrict_f_y(15)*@trend + resids_f_y_b
else
if !totallag = 13 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(15) +
coef_restrict_t_y(16)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(15) +
coef_restrict_f_y(16)*@trend + resids_f_y_b
else
if !totallag = 14 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(16) +
coef_restrict_t_y(17)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(16) +
coef_restrict_f_y(17)*@trend + resids_f_y_b
else
if !totallag = 15 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(17) +
coef_restrict_t_y(18)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(17) +
coef_restrict_f_y(18)*@trend + resids_f_y_b
else
if !totallag = 16 then
```

```
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(18) +
coef_restrict_t_y(19)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(18) +
coef_restrict_f_y(19)*@trend + resids_f_y_b
else
if !totallag = 17 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(19) +
coef_restrict_t_y(20)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(19) +
coef_restrict_f_y(20)*@trend + resids_f_y_b
else
if !totallag = 18 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(20) +
coef_restrict_t_y(21)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(20) +
coef_restrict_f_y(21)*@trend + resids_f_y_b
else
if !totallag = 19 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(21) +
coef_restrict_t_y(22)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(21) +
coef_restrict_f_y(22)*@trend + resids_f_y_b
else
if !totallag = 20 then
a.append dy_t_b = coef_restrict_t_y(1)*x1(-1) + dify_ty_b + dify_tx_b + coef_restrict_t_y(22) +
coef_restrict_t_y(23)*@trend + resids_t_y_b
a.append dy_f_b = coef_restrict_f_y(1)*y_f_b(-1) + dify_fy_b + dify_fx_b + coef_restrict_f_y(22) +
coef_restrict_f_y(23)*@trend + resids_f_y_b
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif
endif

a.append y_t_b = y_t_b(-1) + dy_t_b
a.append y_f_b = y_f_b(-1) + dy_f_b

a.scenario "actuals"
a.solve

    smpl %firstperiod %lastperiod
    equation bootstrap_t_y.ls dy_t_b y_t_b(-1) x1(-1) dy_t_b(-1 to -!opt_p) dx1(-1 to -!opt_q) c @trend
    scalar tstat_b = bootstrap_t_y.@tstat(1)

    tstat_b_dist(!ib) = tstat_b

    smpl %firstperiod %lastperiod
    equation bootstrap_f_y.ls dy_f_b y_f_b(-1) x1(-1) dy_f_b(-1 to -!opt_p) dx1(-1 to -!opt_q) c @trend
```

```
    freeze(mode=overwrite,  fstat_x_b_table) bootstrap_f_y.wald c(2)=0
    scalar fstat_b = @val(fstat_x_b_table(7,2))

    fstat_b_dist(lib) = fstat_b
    next
endif
endif
endif
endif
```